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MODULE TCommit
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This specification is explained in "Transaction Commit", Lecture 5 of the TLA+ Video Course.

Constant RM

The set of participating resource managers

Variable rmState

rmState[rm] is the state of resource manager r.

## $TCTypeOK \triangleq$

The type-correctness invariant

 $rmState \in [RM \rightarrow \{\text{"working"}, \text{"prepared"}, \text{"committed"}, \text{"aborted"}\}]$ 

$$TCInit \stackrel{\triangle}{=} rmState = [r \in RM \mapsto "working"]$$

The initial predicate.

 $canCommit \triangleq \forall r \in RM : rmState[r] \in \{\text{"prepared"}, \text{"committed"}\}$ 

True iff all RMs are in the "prepared" or "committed" state.

 $notCommitted \triangleq \forall r \in RM : rmState[r] \neq "committed"$ 

True iff no resource manager has decided to commit.

We now define the actions that may be performed by the RMs, and then define the complete next-state action of the specification to be the disjunction of the possible RM actions.

$$Prepare(r) \stackrel{\triangle}{=} \land rmState[r] = \text{"working"}$$
  
  $\land rmState' = [rmState \text{ EXCEPT } ![r] = \text{"prepared"}]$ 

$$\begin{array}{ccc} Decide(r) & \stackrel{\Delta}{=} & \vee \wedge rmState[r] = \text{``prepared''} \\ & \wedge canCommit \end{array}$$

 $\land \mathit{rmState'} = [\mathit{rmState} \ \mathtt{EXCEPT} \ ![r] = "\mathsf{committed"}]$ 

 $\lor \land rmState[r] \in \{ \text{"working"}, \text{"prepared"} \}$  $\land notCommitted$ 

 $\land$  notCommittee

 $\land \mathit{rmState}' = [\mathit{rmState} \ \mathtt{EXCEPT} \ ![r] = \texttt{``aborted''}]$ 

 $\mathit{TCNext} \ \stackrel{\triangle}{=} \ \exists \ r \in \mathit{RM} : \mathit{Prepare}(r) \lor \mathit{Decide}(r)$ 

The next-state action.

## $TCConsistent \triangleq$

A state predicate asserting that two RMs have not arrived at conflicting decisions. It is an invariant of the specification.

$$\begin{array}{c} \forall\, r1,\, r2 \in RM: \neg \wedge \mathit{rmState}[r1] = \text{``aborted''} \\ \qquad \qquad \wedge \mathit{rmState}[r2] = \text{``committed''} \end{array}$$

The following part of the spec is not discussed in Video Lecture 5. It will be explained in Video Lecture 8.

 $TCSpec \stackrel{\Delta}{=} TCInit \wedge \Box [TCNext]_{rmState}$ 

The complete specification of the protocol written as a temporal formula.

## THEOREM $TCSpec \Rightarrow \Box (TCTypeOK \land TCConsistent)$

This theorem asserts the truth of the temporal formula whose meaning is that the state predicate  $TCTypeOK \wedge TCInvariant$  is an invariant of the specification TCSpec. Invariance of this conjunction is equivalent to invariance of both of the formulas  $\mathit{TCTypeOK}$  and  $\mathit{TCConsistent}$ .

- $\ \backslash \ ^* \ \mathrm{Modification} \ \mathrm{History}$
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